
Physical models for nanowire device simulation

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ESSDERC/ ESSCIRC Workshop "Process Variations from Equipment Effects to Circuit and Design Impacts"

September 3, 2018, Dresden, Germany

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Outline

- Introduction
 - Project flow and link between the Work Packages
- Physical models and methods
 - Drift Diffusion Method (DD)
 - Kubo-Greenwood
 - Non-Equilibrium Green's Function (NEGF)
 - Wigner Monte Carlo
- Conclusions and outlook

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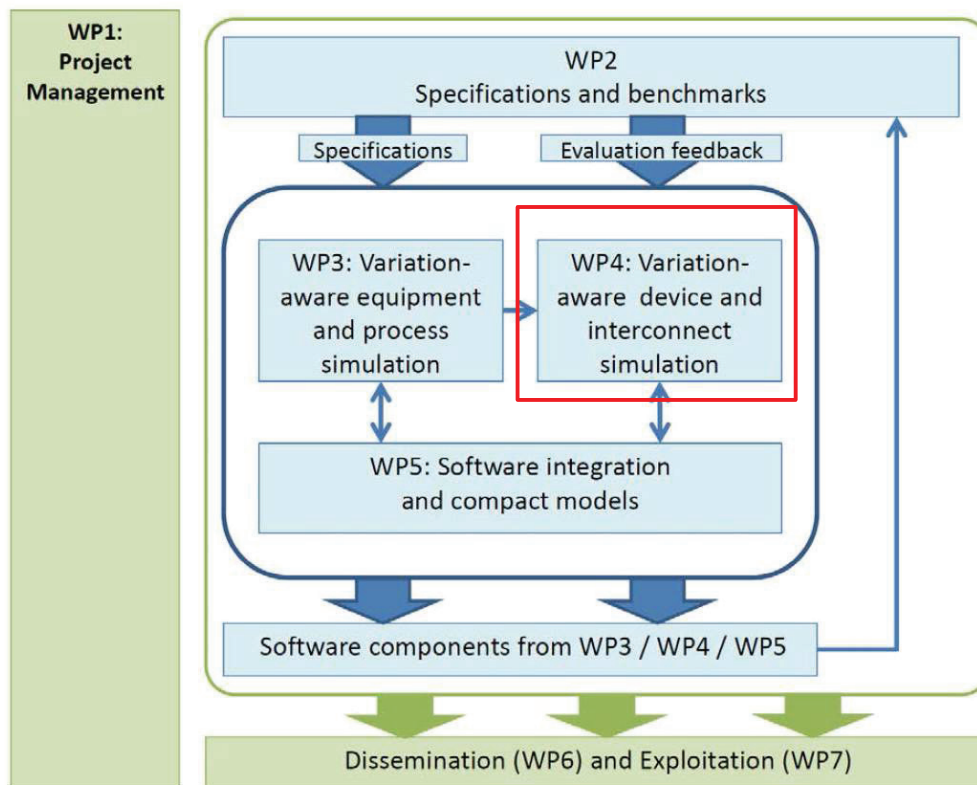


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Introduction - Project Context



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Introduction - Goals and Strategy of WP4

- The objective of this work package is to **enable device and advanced interconnect simulation tools** to deal with **realistic geometries including variability and process-induced variation**.
- **To develop and to implement refined physical models** which are needed for the **simulation of advanced More Moore devices like FinFETS and Nanowire Transistors**, especially when effects of ***confinement, quantum behaviour and charge granularity*** come into play. **Interconnect models** will be developed, which properly account for **grain boundary and surface roughness effects** on electron transport.

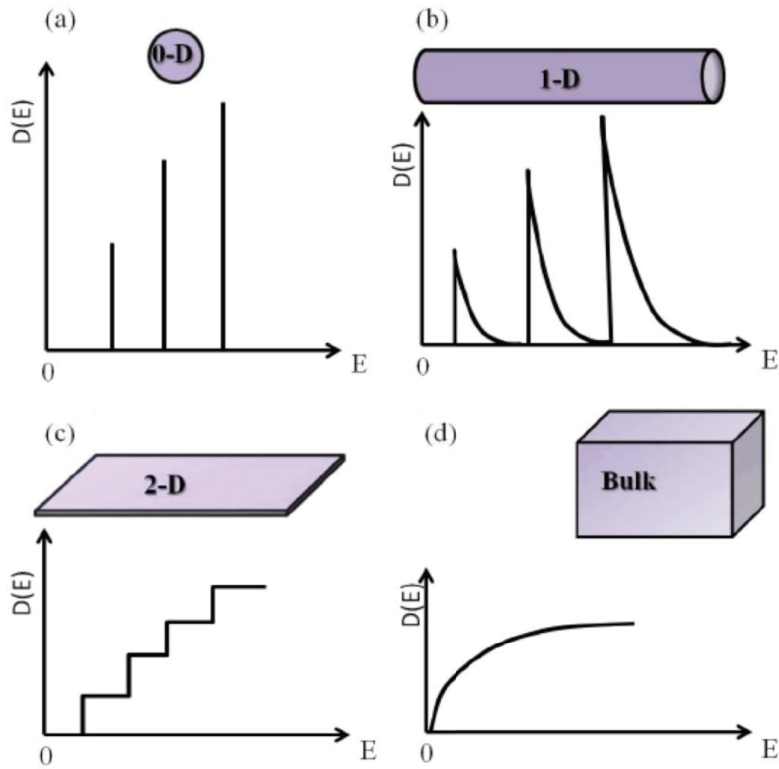
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Introduction - Basic Physics



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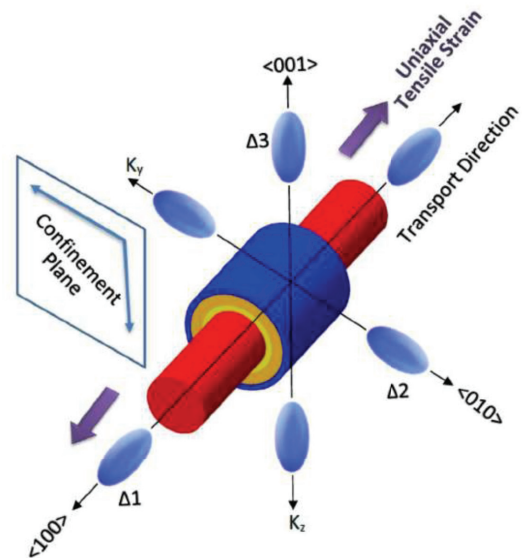
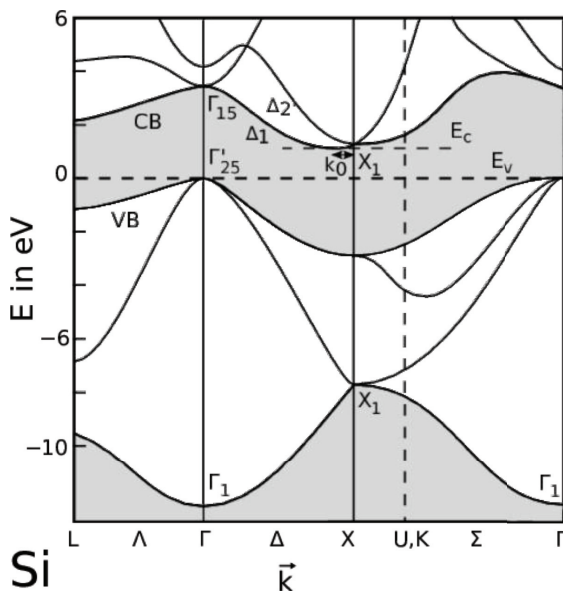


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Introduction - Basic Physics



Conduction band consists of six energy ellipsoids (Δ) along the confinement plane and uniaxial tensile strain.

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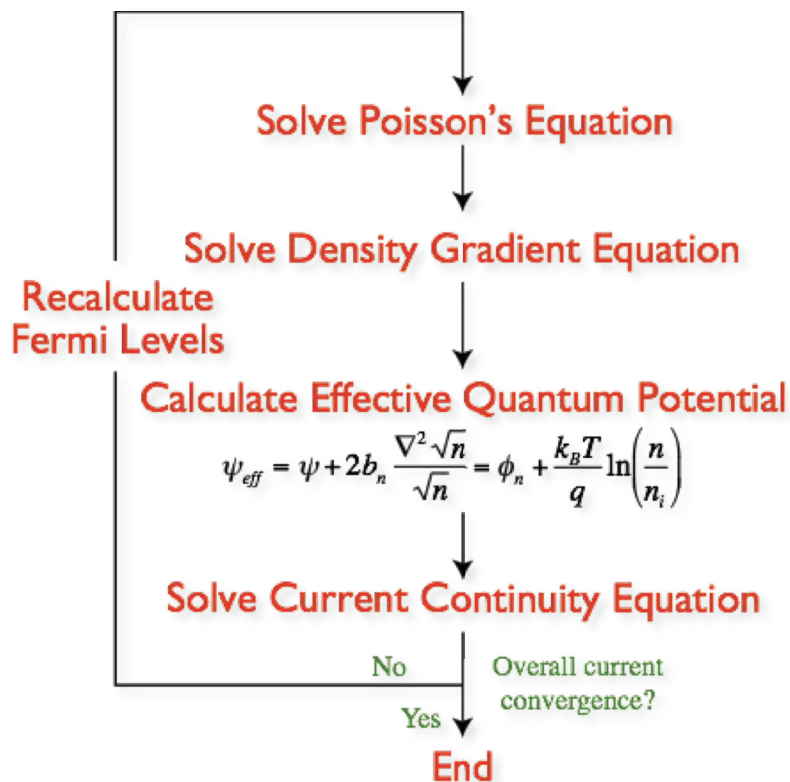


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Physical Model - Drift Diffusion



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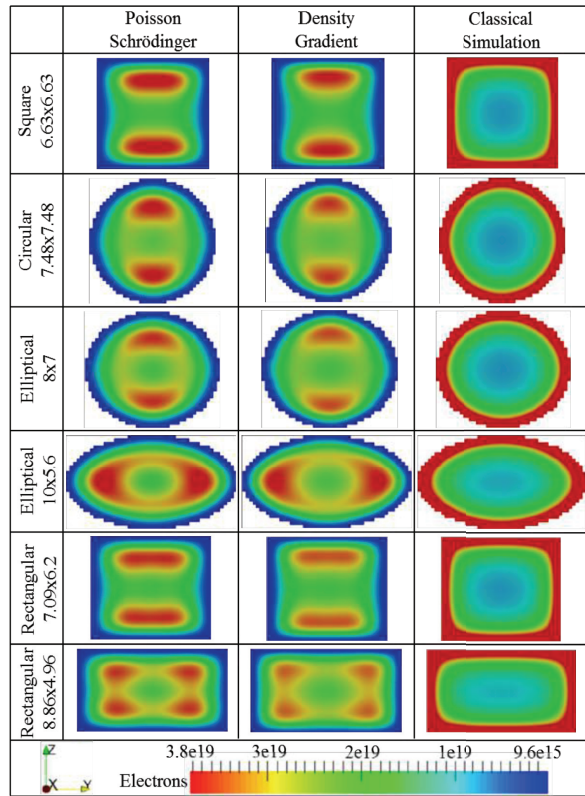
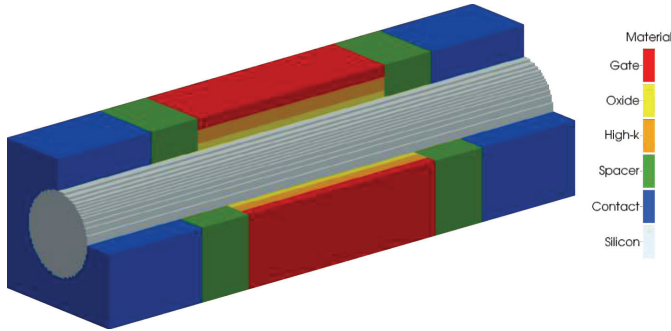
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Physical Model - Drift Diffusion

Parameters	Value
Gate length (nm)	18
Spacer thickness (nm)	5.0
S/D peak doping (cm ⁻³)	2×10 ²⁰
Channel doping (cm ⁻³)	10 ¹⁴
Substrate orientation	(001)
Nanowire orientation	<110>, <100>
T _{oxide} (nm)	0.8



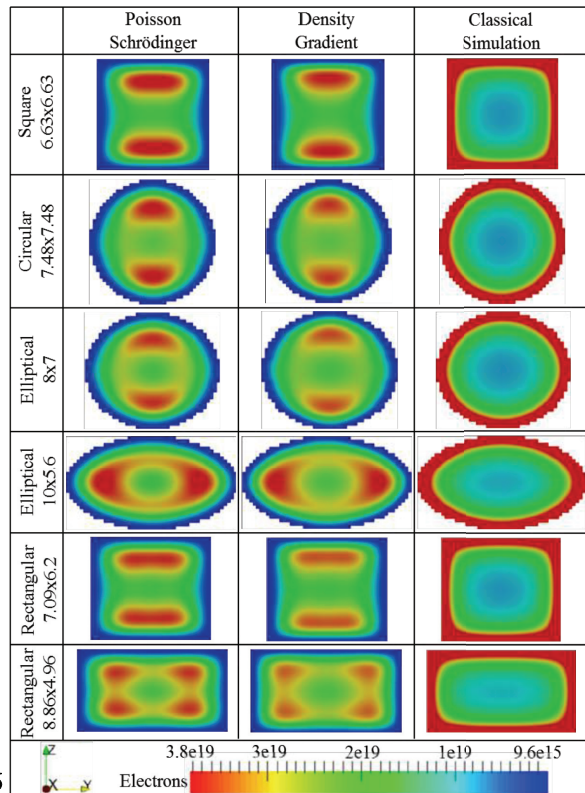
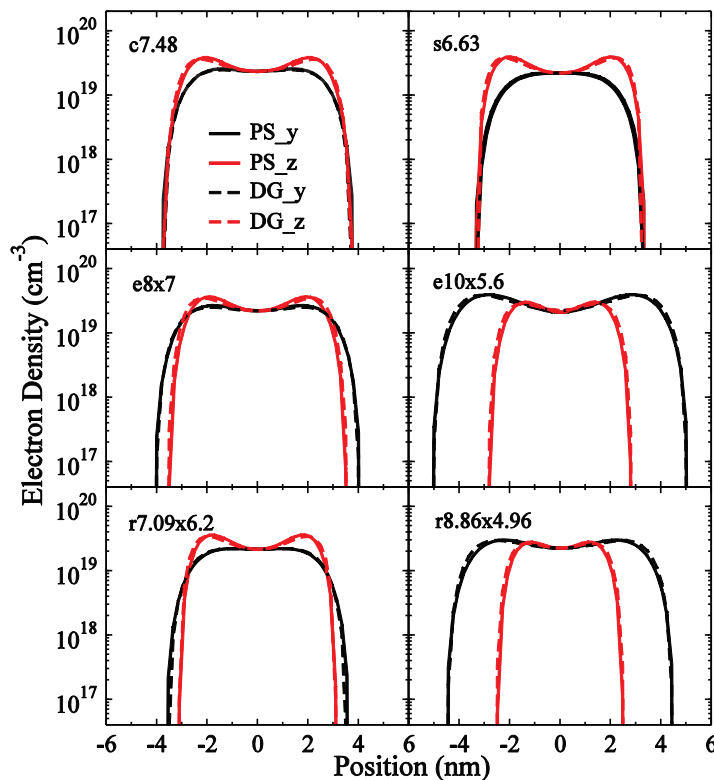
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Physical Model - Drift Diffusion



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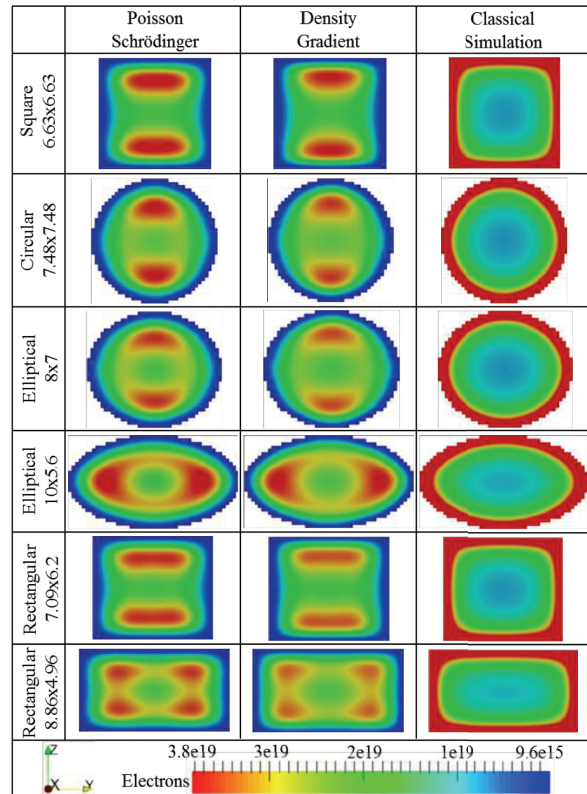


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Physical Model - Drift Diffusion

Device	Q_M ($10^6/cm$)	C_G ($10^{-12}F/cm$)	Q_M/C_G ($10^{18}/F$)
s6.63x6.63	7.208	5.915	1.219
c7.48x7.48	7.670	5.922	1.295
e8x7	8.229	6.171	1.334
e10x5.6	9.638	7.081	1.361
r7.09x6.2	7.971	6.130	1.300
r8.86x4.96	9.104	6.746	1.350
e5.6x10	6.771	6.312	1.073



The change in **shape** can have > 20% impact on performance

The change in **orientation** can have > 30% impact on performance

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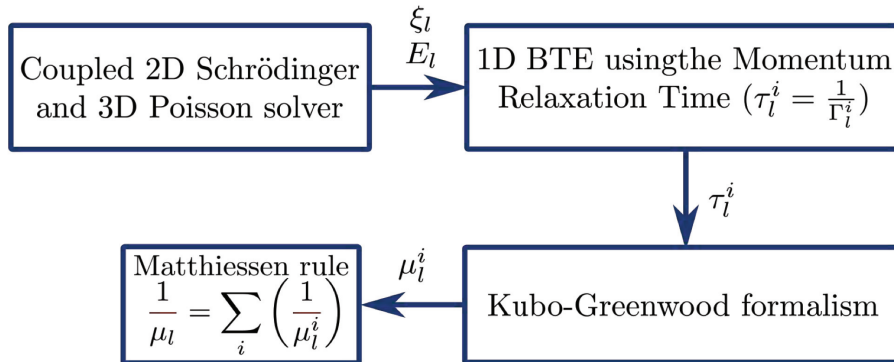
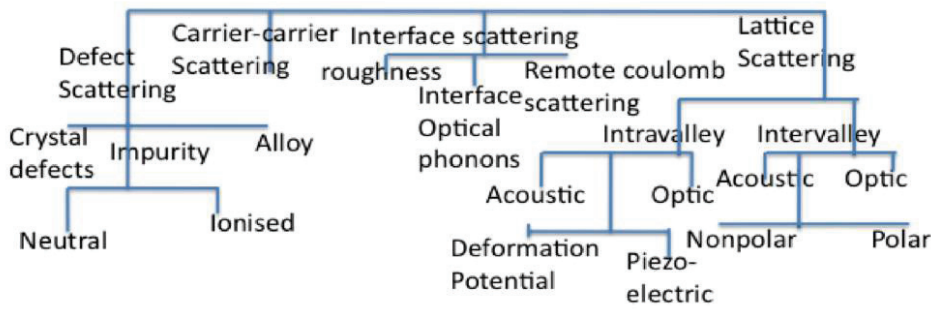
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Physical Model - Kubo-Greenwood

Scattering mechanism



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Physical Model - Kubo-Greenwood

Acoustic Phonon Scattering Mechanism

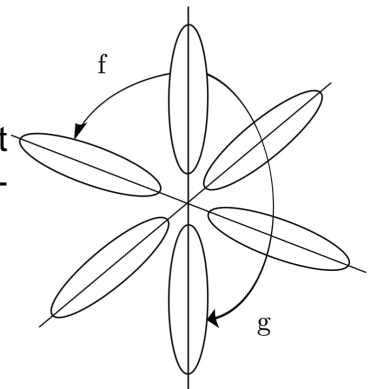
- Elastic and intra-valley transitions are only allowed

Optical Phonon Scattering Mechanism

- Inelastic mechanisms
- The two different transitions among the six equivalent X minima of Si must be considered: g-type (intra-valley) and f-type (inter-valley) processes

Ionized Impurity Scattering Mechanism

- Elastic and intra-valley transitions are only allowed
- Fixed uniform ionized impurity concentration: $n_0 = [10^{17} - 10^{19}] \text{ cm}^{-3}$



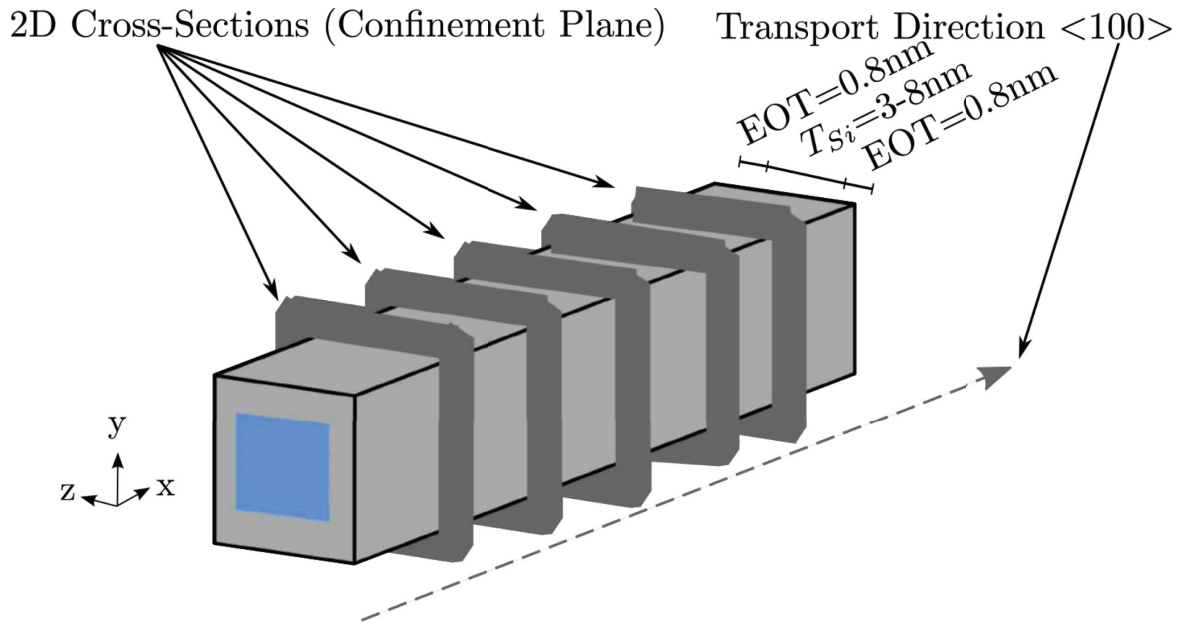
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Physical Model - Kubo-Greenwood



Silicon gate-all-around (GAA) nanowire transistor (NWT) in [100] orientation. Thickness (T) and width (W) range from T=W=3nm to T=W=8nm for square and circular cross-sectional shapes including 20 sub-bands.

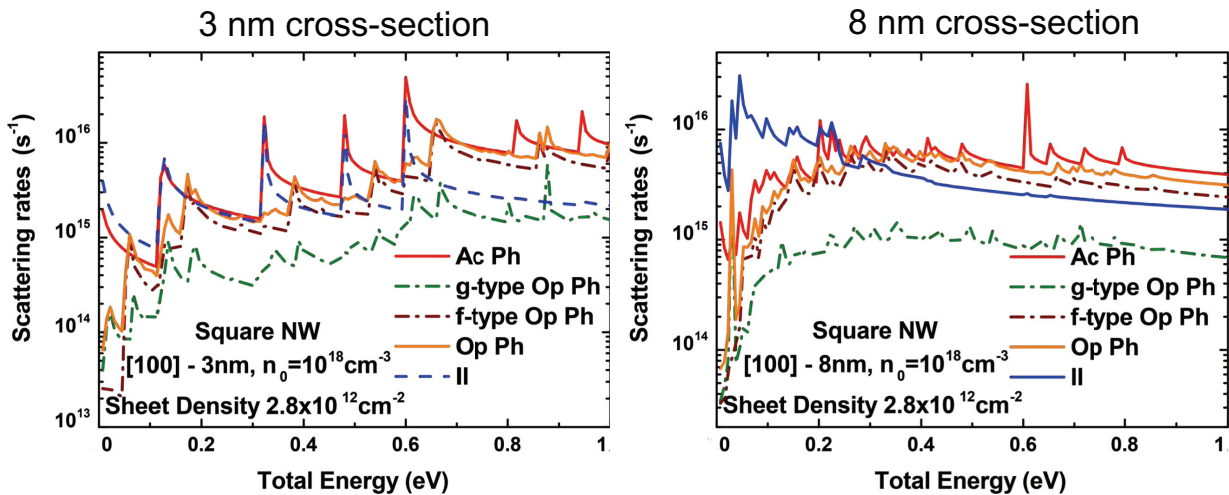
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Physical Model - Kubo-Greenwood



- The multisub-band effects in the scattering rates are generally more pronounced for smaller W.

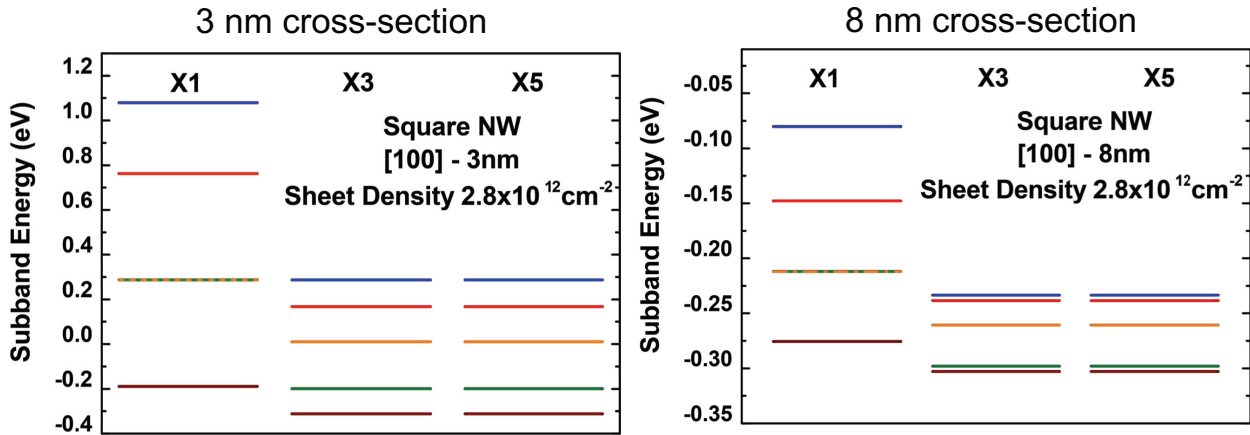
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Physical Model - Kubo-Greenwood



- The multisub-band effects in the scattering rates are generally more pronounced for smaller W.
- Higher energy difference between sub-bands minimizes the electron transitions.

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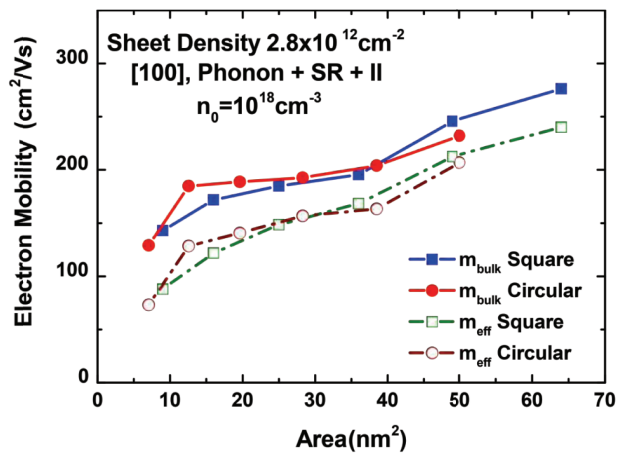
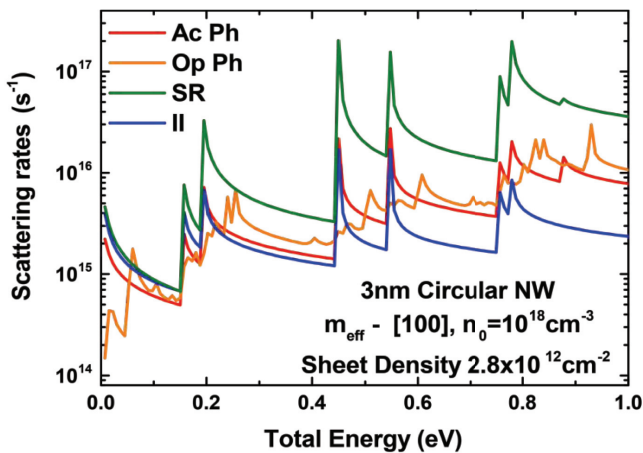
Physical Model - Kubo-Greenwood

Scattering mechanisms:

- Elastic intra-valley acoustic phonon
- g- and f-type optical phonon
- Ionized impurity
- *Surface Roughness*

Si Nanowire transistors [100]:

- Effective mass calculation for each device
- Different width/height: 3nm – 8nm
- Different shape: square and circular



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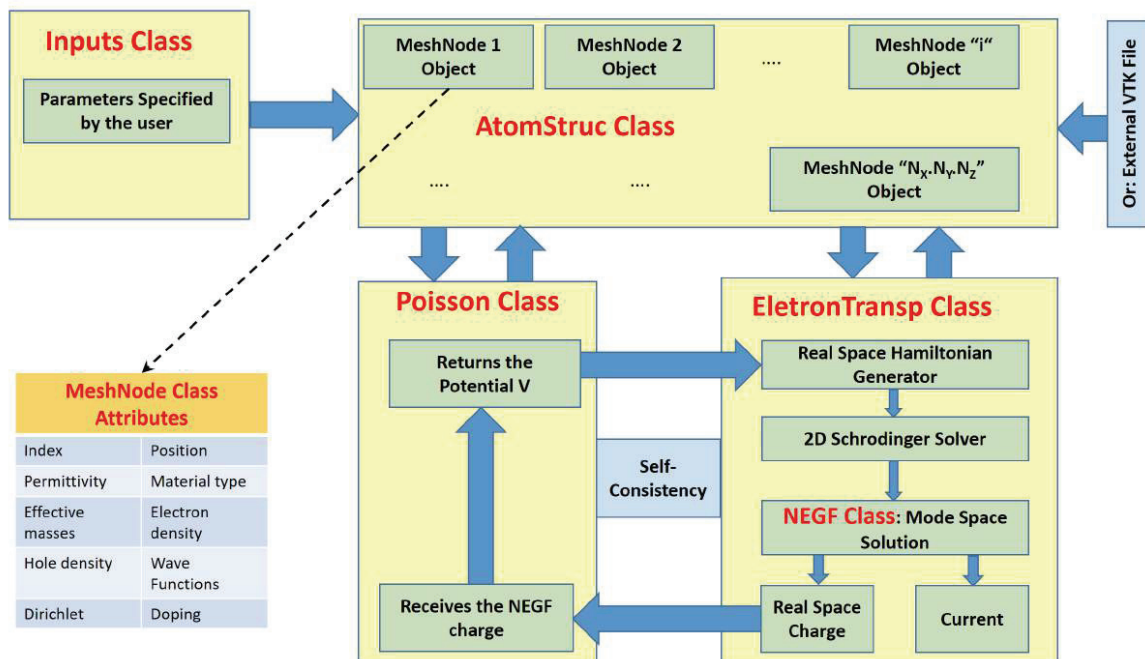
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Physical Model - NEGF



- Nano-Electronic Simulation Software (NESS) - University of Glasgow Device Simulator

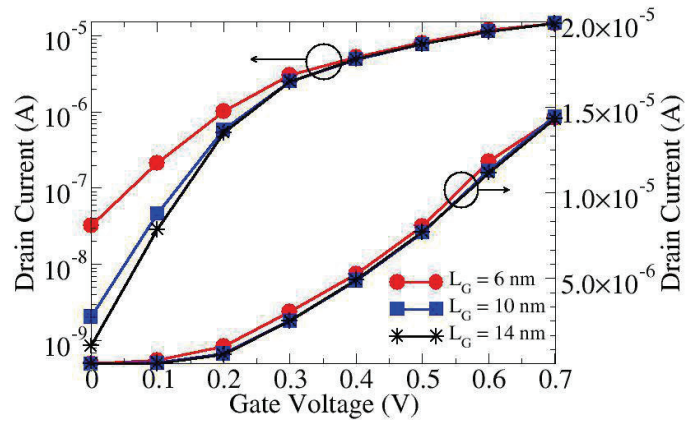
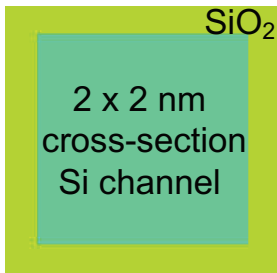
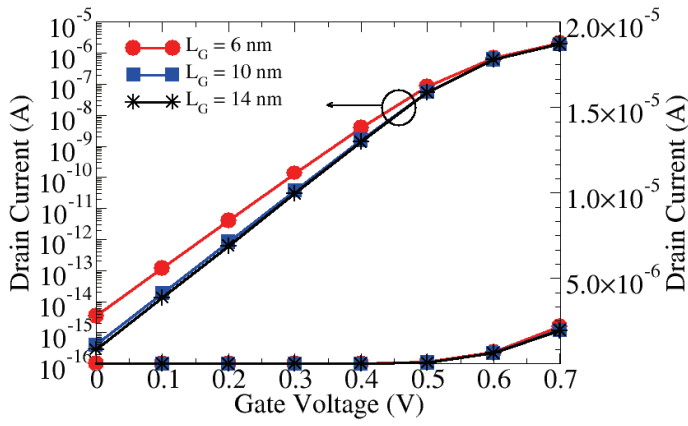
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Physical Model - NEGF



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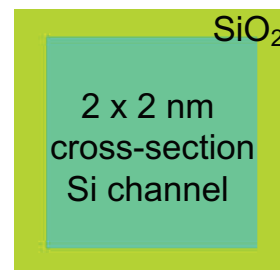
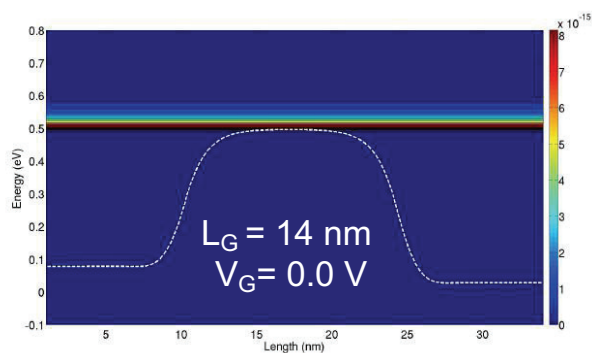
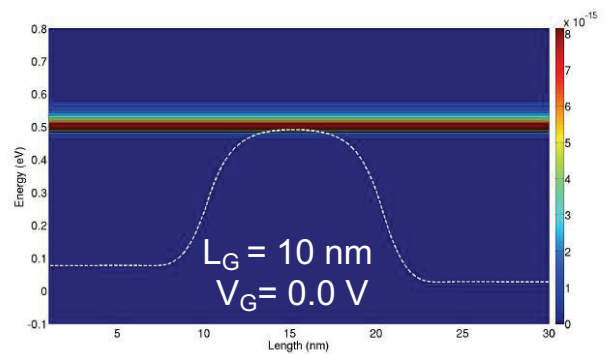
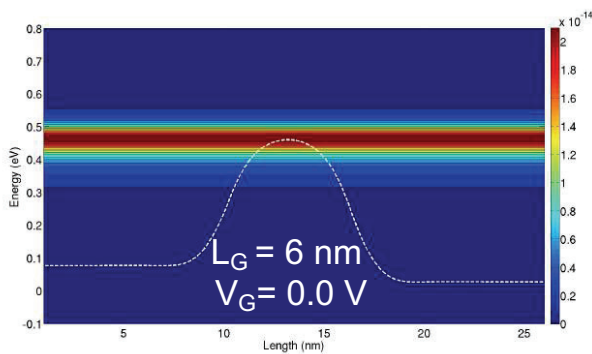


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Physical Model - NEGF



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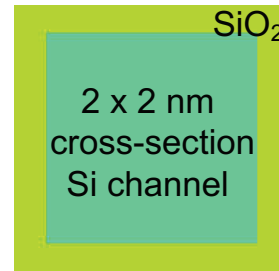
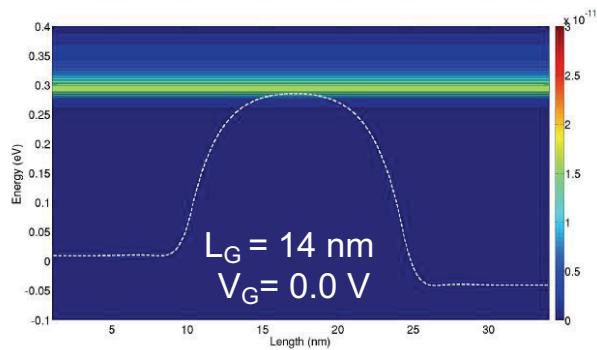
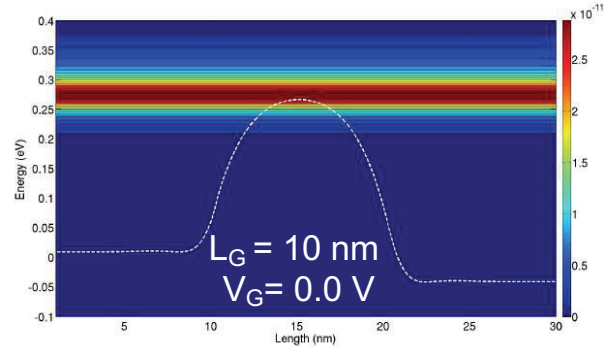
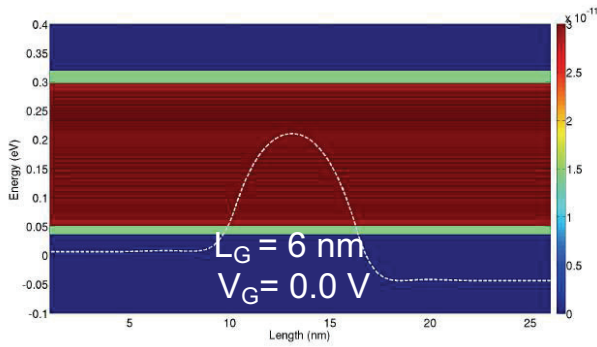


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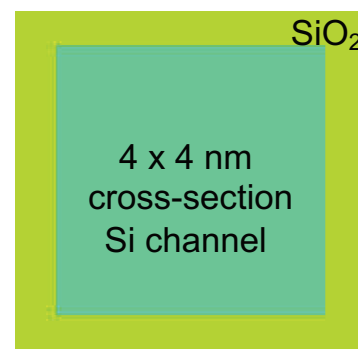
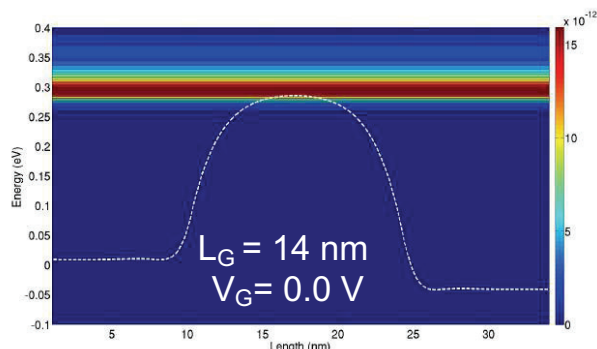
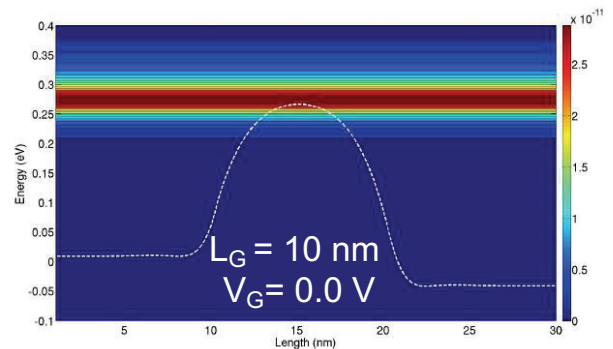
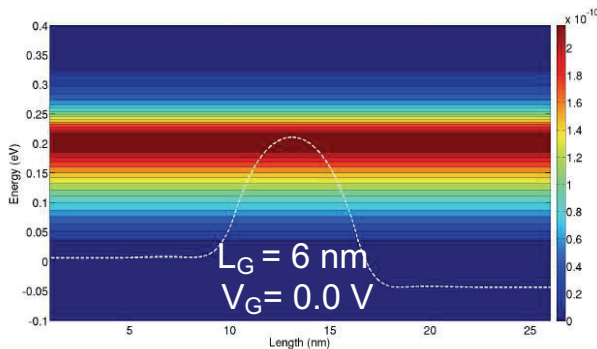


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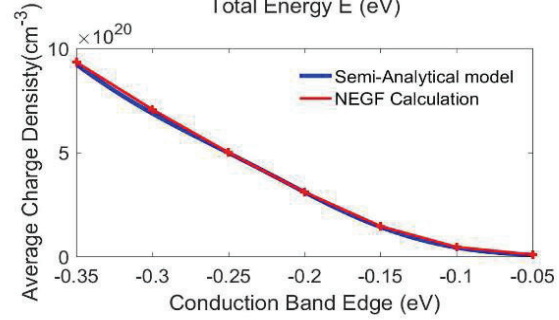
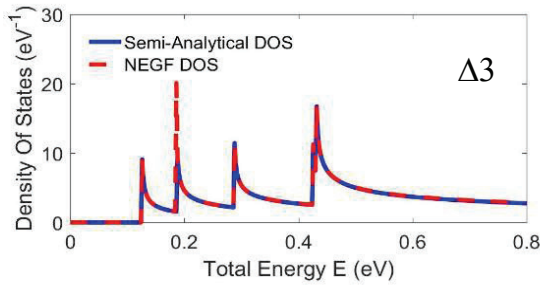
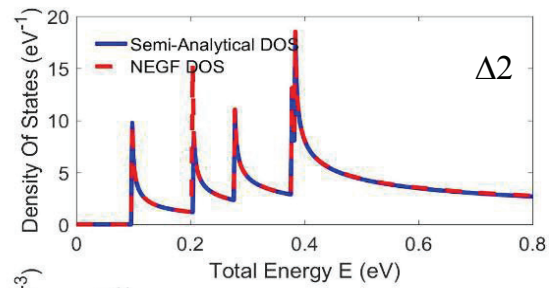
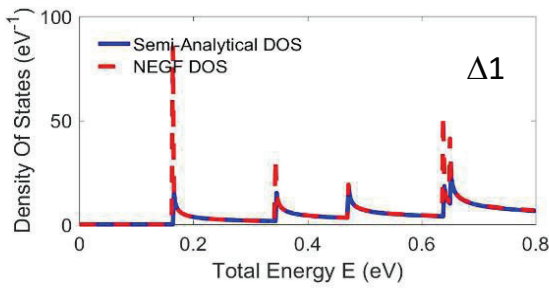
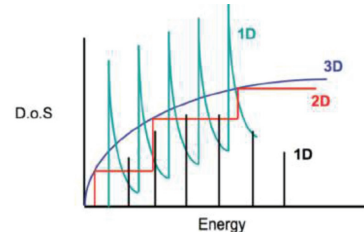
Physical Model - NEGF



Physical Model - NEGF



Physical Model - NEGF



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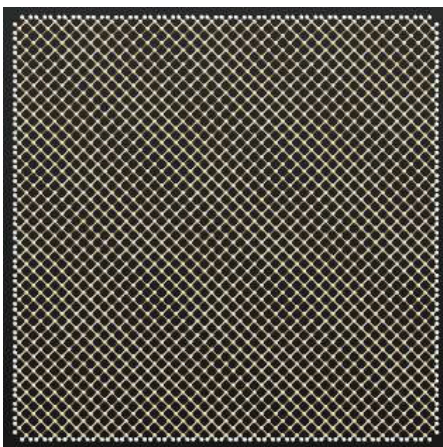


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Physical Model - Band Structure

8nm Square Si NW

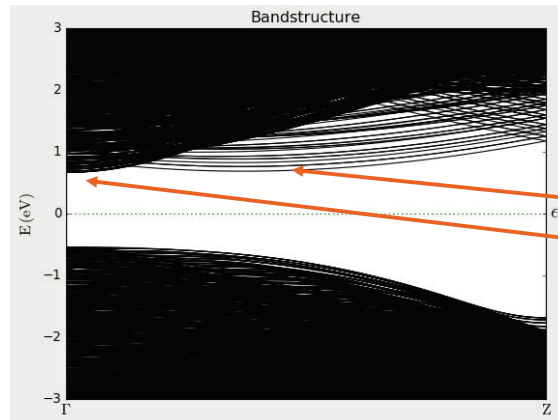


Simulation Method

- **sp3d5s* tight binding** with a Boykin parameter set
- No geometric optimization
- [100] transport direction

From reference [PRB 69 115201 (2004)]

- Effective mass of bulk Si: 0.891, 0.201 m_e (longitudinal, transverse)
- Bandgap: 1.131 eV



Effective mass (parabolic fit)
 m_l : 0.900 m_e
 m_t : 0.215 m_e

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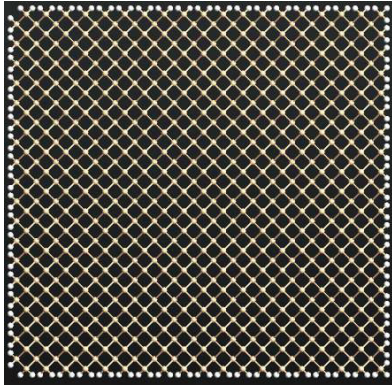


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Physical Model - Band Structure

5nm Square Si NW

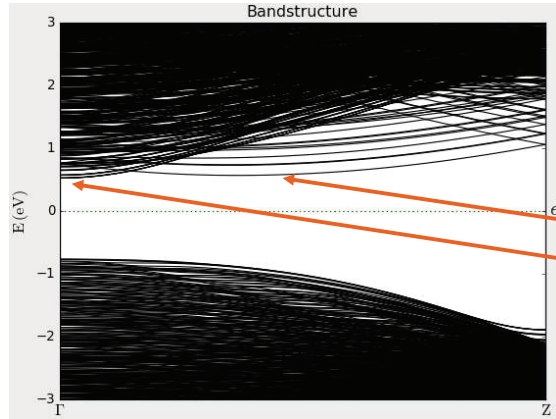


Simulation Method

- ***sp3d5s** tight binding** with a Boykin parameter set
- No geometric optimization
- [100] transport direction

From reference [PRB 69 115201 (2004)]

- Effective mass of bulk Si: 0.891, 0.201 m_e (longitudinal, transverse)
- Bandgap: 1.131 eV



Effective mass (parabolic fit)
 m_l : 0.917 m_e
 m_t : 0.231 m_e

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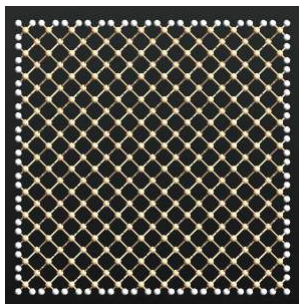


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Physical Model - Band Structure

3nm Square Si NW

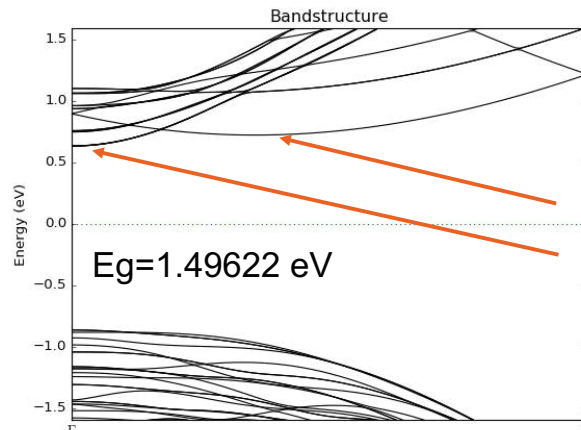


Simulation Method

- ***sp3d5s** tight binding** with a Boykin parameter set
- No geometric optimization
- [100] transport direction

From reference [PRB 69 115201 (2004)]

- Effective mass of bulk Si: 0.891, 0.201 m_e (longitudinal, transverse)
- Bandgap: 1.131 eV



Effective mass (parabolic fit)
 m_l : 0.951 m_e
 m_t : 0.268 m_e

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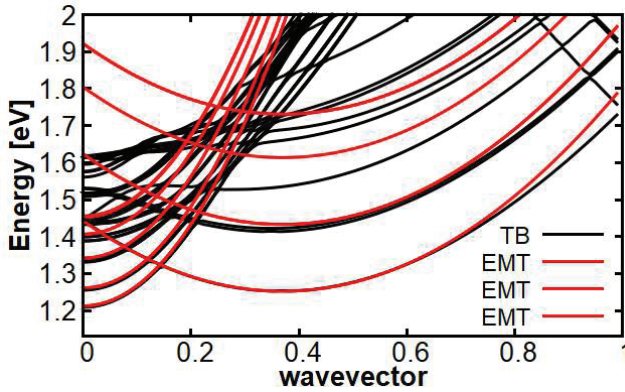
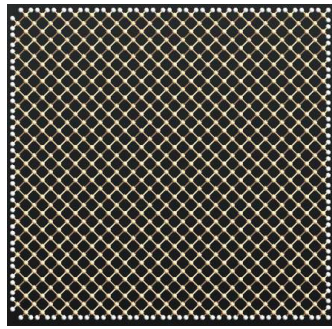


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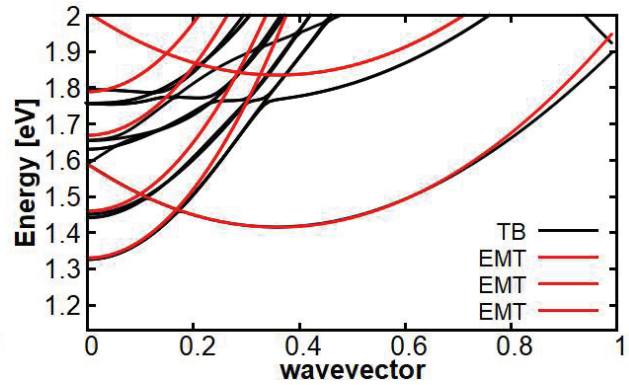
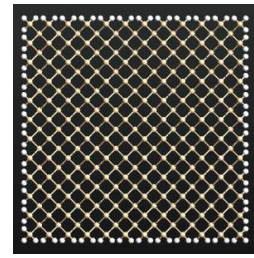


Physical Model - Band Structure

5nm Square Si NW



3nm Square Si NW



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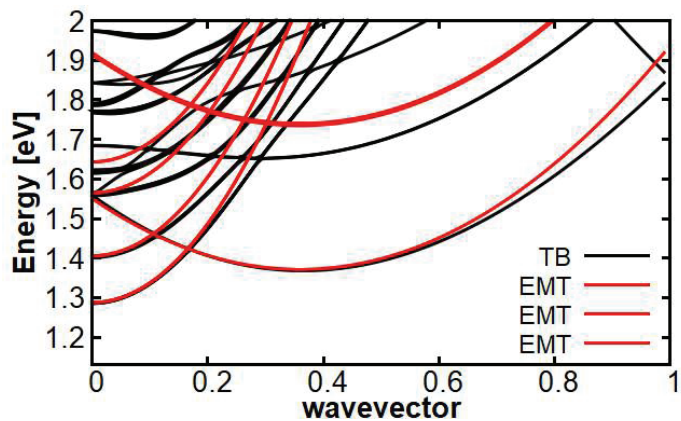
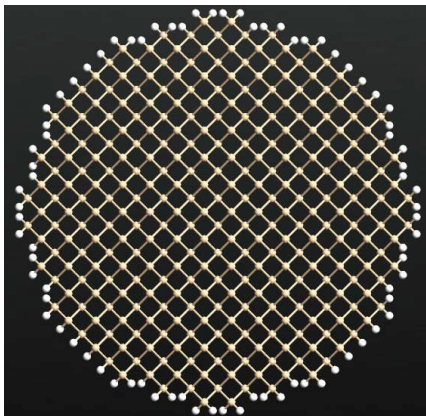


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Physical Model - Band Structure (Task 4.1.4)



Atomic structure of Si NW (3.82 nm)

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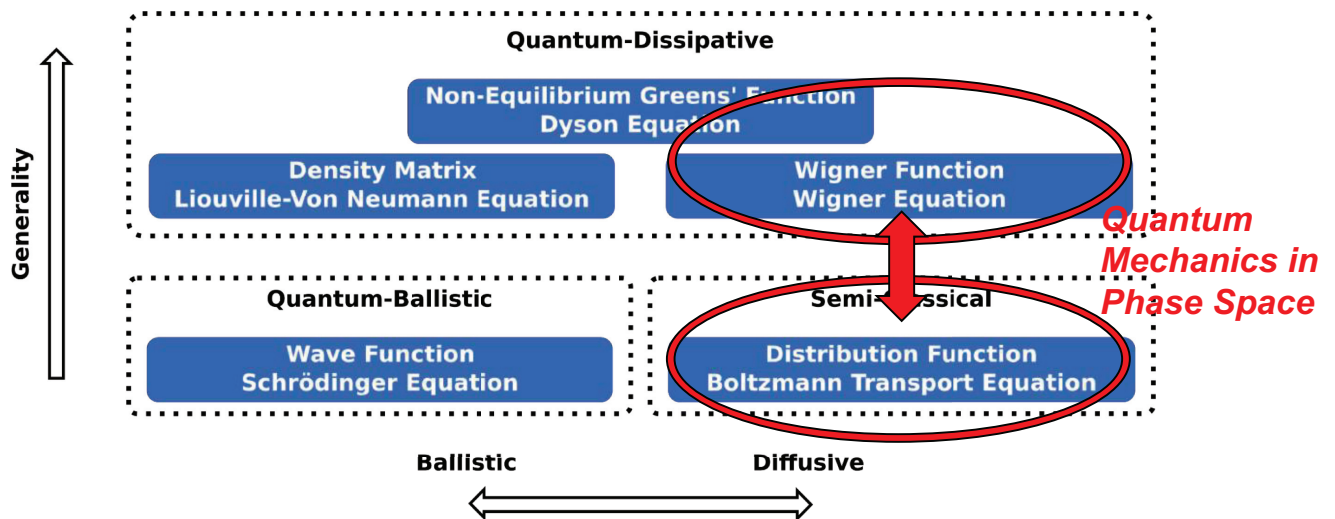


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Physical Model - Wigner MC



Signed particle approach supports switching between

- Quantum particle evolution: Wigner transport
- Classical particle evolution: Boltzmann transport

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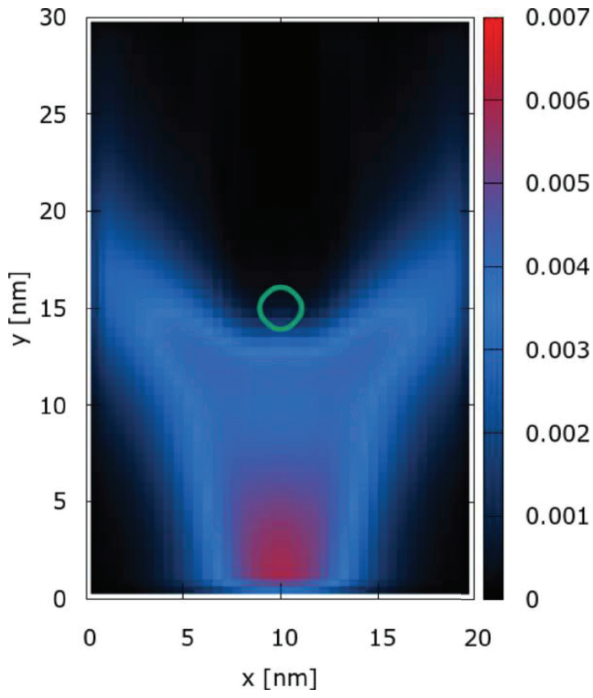


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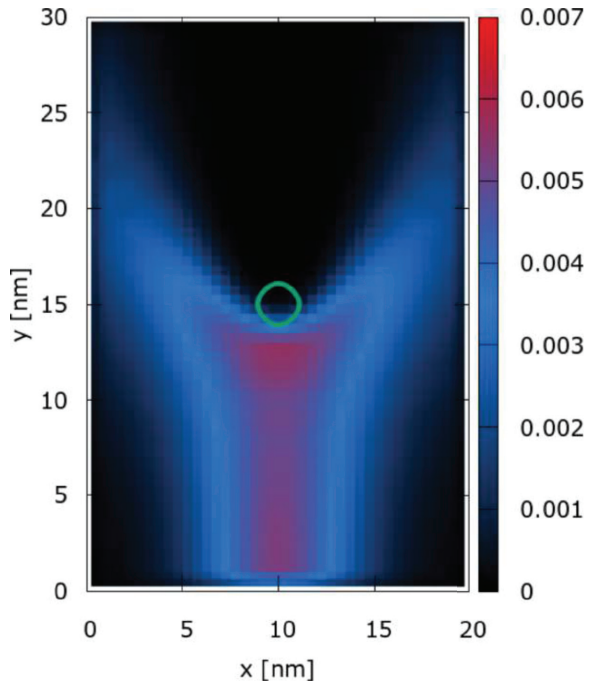


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Physical Model - Wigner MC



Quantum electron density [a.u.]



Classical electron density [a.u.]

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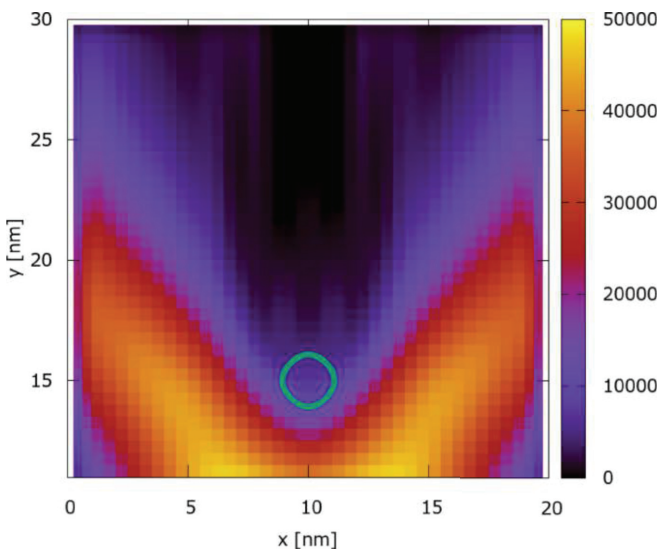
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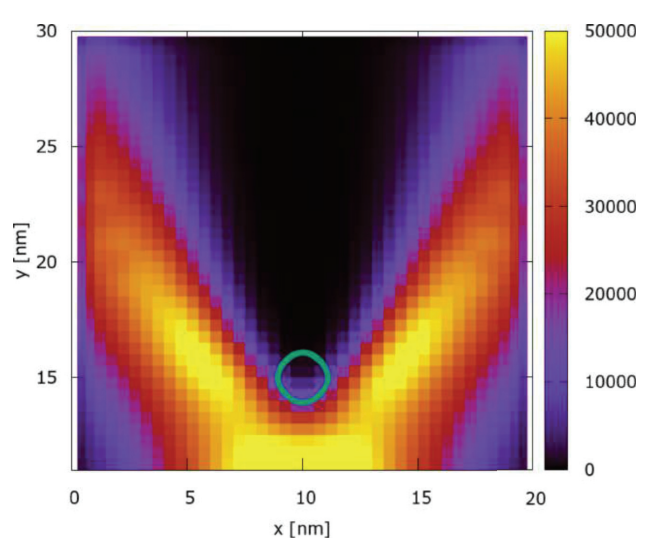
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Physical Model - Wigner MC



Quantum current density [a.u.]



Classical current density [a.u.]

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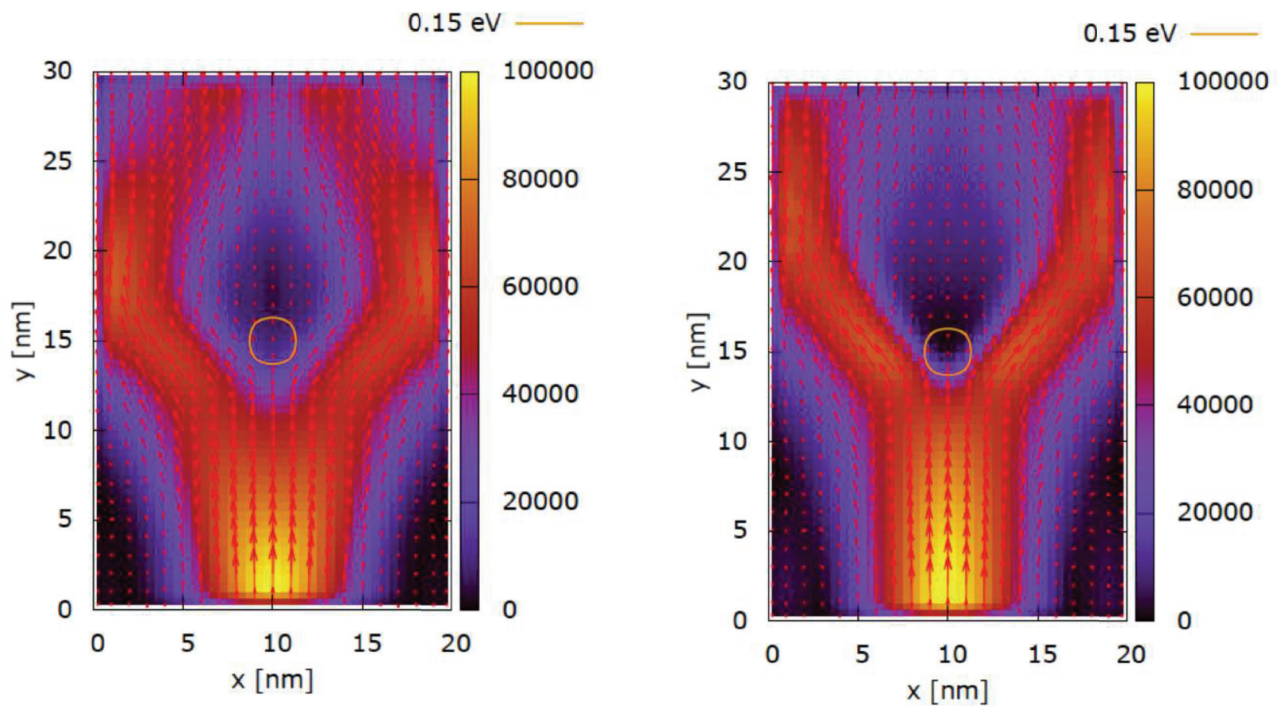
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Physical Model - Wigner MC



With lateral reflecting boundaries

Quantum current density [a.u.]

Classical current density [a.u.]

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Conclusions and Outlook

- Physical models and methods
 - Drift Diffusion Method (DD)
 - Fast and well established method but needs quantum corrections
 - Kubo-Greenwood
 - Particle statistical method, needs the appropriate scattering models, good for evaluating mobility in the devices
 - Non-Equilibrium Green's Function (NEGF)
 - Wave representations of the carriers, able to capture quantum mechanical tunneling
 - Wigner Monte Carlo
 - Particle statistical method, quantum mechanics in phase space

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SUPERAID7 Workshop "Process Variations from Equipment Effects to Circuit and Design Impacts" September 3, 2018, Dresden



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